**Hess's Law:** The value of  $\Delta H$  for any reaction that can be written in steps equals the sum of the values of  $\Delta H$  for the individual steps.

# Method 1: Additivity of Heats

1. Identify the target equation and balanced it (if not given).

2. Identify the individual step equations. These are provided or are found on a Table of Heats of Formation.

3. Reverse any step equations so that the position of reactants/products matches that of the target equation. If an equation is reversed, also reverse the sign of  $\Delta H$  for the step equation.

4. Multiply the step equations by the appropriate coefficient to match those in the target equation. Also multiply the  $\Delta H$  by the same coefficient.

5. Add up the modified step equations and their  $\Delta H$  values. The sum of the modified individual step equation should be identical to the target equation.

Heats (Enthalpy Change) of Formation		
Image: Constraint of the second system         Formula           H2 (g) + ½ O2 (g) $\rightarrow$ H2O (g)           H2 (g) + ½ O2 (g) $\rightarrow$ H2O (l)           S (s) + ½ O2 (g) $\rightarrow$ SO2 (g)           S (s) + ½ O2 (g) $\rightarrow$ SO3 (g)           H2(g) + S(s) + 2O2(g) $\rightarrow$ H2SO4 (l)           ½ N2 (g) + ½ O2 (g) $\rightarrow$ NO (g)           ½ N2 (g) + ½ O2 (g) $\rightarrow$ NO2 (g)           ½ N2 (g) + ½ O2 (g) $\rightarrow$ NO2 (g)           ½ N2 (g) + ½ O2 (g) $\rightarrow$ NO2 (g)           ½ N2 (g) + ½ O2 (g) $\rightarrow$ CO (g)           C (s) + ½ O2 (g) $\rightarrow$ CO (g)           C (s) + ½ O2 (g) $\rightarrow$ CO (g)           C (s) + ½ O2 (g) $\rightarrow$ CO2 (g)           C (s) + ½ O2 (g) $\rightarrow$ CO2 (g)           C (s) + ½ O2 (g) $\rightarrow$ CO2 (g)           C (s) + 1/2 O2 (g) $\rightarrow$ CO2 (g)           C (s) + 2H2 (g) $\rightarrow$ CO2 (g)           C (s) + 2H2 (g) $\rightarrow$ CO2 (g)           C (s) + 3H2 (g) $\rightarrow$ CO2 (g)           C (s) + 3H2 (g) $\rightarrow$ C2H6 (g)           C (s) + 4H2 (g) + O2 (g) $\rightarrow$ C3H7COOH (l)           2C (s) + 4H2 (g) + O2 (g) $\rightarrow$ C3H7COOH (l)           2C (s) + 2H2 (g) + O2 (g) $\rightarrow$ CH3COOH (l)	Name water vapour water sulfur dioxide sulfur trioxide sulfuric acid nitric oxide nitrogen dioxide ammonia carbon monoxide carbon dioxide methane ethane propane hydrogen iodide butyric acid	- 811.7 + 90.25 + 33.18 - 46.11 - 110.5 - 393.5 - 74.81 - 84.68 - 103.8

### Method 1: Additivity of Heats (continued)

**Example:** Determine  $\Delta H$  for the following reaction: methane (g) + oxygen (g)  $\longrightarrow$  carbon dioxide (g) + water (g)

## **Method 2: Summation of Heats**

Identify the  $\Delta H_{\text{formation}}$  for each product and reactant and solve using the equation:

$$\Delta H = \sum \left( n \Delta H_{form}(products) \right) - \sum \left( n \Delta H_{form}(reactants) \right)$$

**Example:** Determine  $\Delta H$  for the following reaction: ammonia (g) + oxygen (g)  $\longrightarrow$  nitrogen dioxide (g) + water (g) NH<sub>3</sub> (g) +  $\frac{7}{4}$  O<sub>2</sub>  $\longrightarrow$  NO<sub>2</sub> (g) +  $\frac{3}{2}$  H<sub>2</sub>O (g) SCH4U1

#### Hess's Law and Additivity of Heats

# Complete these questions using the Additivity of Heats method. Refer to the Table of Heats of Formation for the individual step equations.

- 1. Calculate  $\Delta H$  for each of the following:
  - a)  $H_2O(I) \longrightarrow H_2O(g)$ b)  $C_3H_7COOH(I) + 5O_2(g) \longrightarrow 4CO_2(g) + 4H_2O(I)$ c)  $3 CH_3COOH(I) + \frac{11}{2}O_2(g) \longrightarrow 5CO_2(g) + CO(g) + 6H_2O(I)$
- a) Write a balanced equation for the combustion of propane gas (C<sub>3</sub>H<sub>8</sub>) to produce carbon dioxide and water vapour.
  b) Add equations and heats of formation to calculate the Δ*H* for the combustion of 1.00 mol of propane.
- Answers: 1 a) 44.0 kJ/mol b) -2195 kJ/mol c) -2333 kJ/mol 2 -2044 kJ

#### Do the following problems using the Summation of Heats method.

1. Predict the heat of reaction for:

 $CH_4(g) + 2O_2(g) \longrightarrow CO_2(g) + 2H_2O(g)$ 

2. Given that  $\Delta H_{\text{form}}$  for SiO<sub>2</sub> (s) is – 856.9 kJ/mol, what is the  $\Delta H$  for:

 $SiO_2(s) + C(s) \longrightarrow CO_2(g) + Si(s)$ 

- 3. What is the heat of formation of  $H_2SO_4$  (I) from  $H_2O$  (I) and  $SO_3$  (g)?
- 4. Given:  $\Delta H_{\text{form}} \text{ for } P_4O_{10} (s) = -3009.5 \text{ kJ/mol} \\ \Delta H_{\text{form}} \text{ for } H_3PO_4 (s) = -1266.5 \text{ kJ/mol}$

Calculate the heat of reaction for:  $P_4O_{10}(s) + 6H_2O(l) \longrightarrow 4H_3PO_4(s)$ 

Answers: 1. - 802.3 kJ/mol 2. + 463.4 kJ/mol 3. - 130.2 kJ/mol 4. - 342 kJ/mol