

Huygens, Hooke and Young

1665 – Robert Hooke proposed the wave theory of light, a sharp contrast to Newton's accepted particle theory.

~ 1685 - Christiaan Huygens added to wave theory:

Huygen's Principle:

Every point on a wave front can be considered as a point source of tiny secondary wavelets that spread out in front of the wave, with the same speed and frequency as the wave itself.

Huygen's principle explains why diffraction occurs:

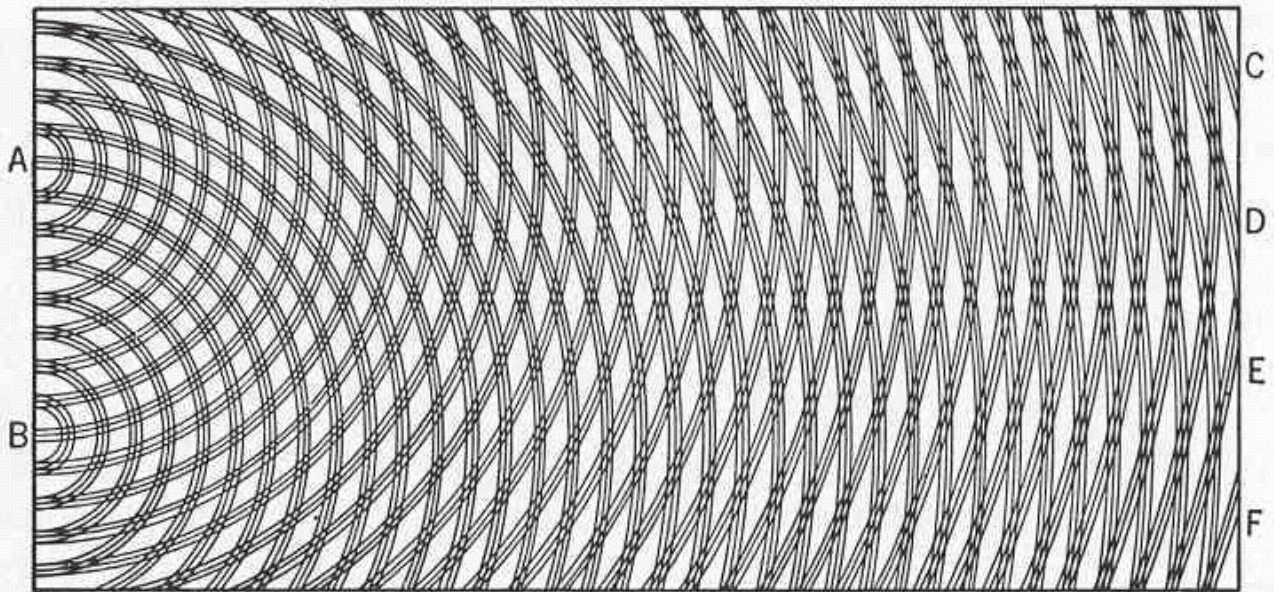
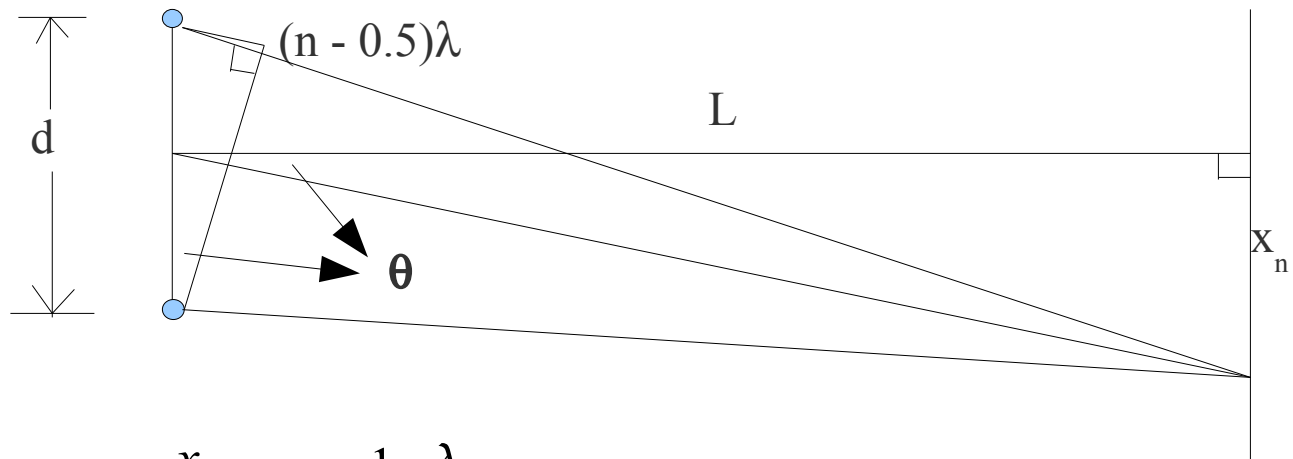


FIG. 1

Wavelets at A and B are identical, so interference is seen on the screen at CDEF (nodes/antinodes).



$$\sin \theta_n = \frac{x_n}{L} = \left(n - \frac{1}{2}\right) \frac{\lambda}{d} \quad (\text{because } \sin \sim \tan \text{ for small angles})$$

where $n = 1, 2, 3 \dots$

The above formula works for dark fringes (nodal) ONLY!!

For bright fringes,

$$\sin \theta_n = \frac{x_n}{L} = \frac{n \lambda}{d}$$

and from the above relationships we can derive an equation for the distance between successive nodes (or antinodes),

$$x_n = \left(n - \frac{1}{2}\right) \frac{L \lambda}{d}, \text{ so}$$

$$x_{n+1} - x_n = \left(n + 1 - \frac{1}{2}\right) \frac{L \lambda}{d} - \left(n - \frac{1}{2}\right) \frac{L \lambda}{d}$$

$$\Delta x = \frac{L \lambda}{d}$$

Examples:

1. A laser is used in Young's double-slit experiment and produces a fourth order nodal fringe at an angle of 4° . Find the wavelength of the light if the slits are 0.05 mm apart.

$$\sin \theta_n = \left(n - \frac{1}{2}\right) \frac{\lambda}{d}$$

$$\sin 4^\circ = \left(4 - \frac{1}{2}\right) \frac{\lambda}{5 \times 10^{-5}}$$

$$\lambda = 9.97 \times 10^{-7} \text{ m} \quad (\text{note} - \text{this is not visible light})$$

2. Monochromatic light falls on two narrow slits 0.07 mm apart. Successive antinodal fringes are seen 4 cm apart on a screen 4.3 m away. Determine the wavelength of the light.

$$\Delta x = \frac{L \lambda}{d}$$

$$4 \times 10^{-2} = \frac{(4.3) \lambda}{7 \times 10^{-5}}$$

$$\lambda = 6.5 \times 10^{-7} \text{ m}$$