

## More Practice with Collisions in 2D

### SPH4U

1. A steel ball of mass 0.50 kg, moving with a velocity of 2.0 m/s [E], strikes a second ball of mass 0.30 kg, initially at rest. The collision is a glancing one, causing the steel ball to have a velocity of 1.5 m/s [ $30^\circ$  N of E] after the collision. Determine the velocity of the second ball after the collision.

$$m_A = 0.50 \text{ kg} \qquad v_A = 2.0 \frac{\text{m}}{\text{s}} [E] \qquad v_A' = 1.5 \frac{\text{m}}{\text{s}} [30^\circ \text{ N of } E]$$

$$m_B = 0.30 \text{ kg} \qquad v_B = 0 \frac{\text{m}}{\text{s}} \qquad v_B' = ?$$

Determine the total East-West ( $x$ ) and North-South ( $y$ ) components of the momentum before:

$$p_{TOTALx} = m_A v_{Ax} + m_B v_{Bx} =$$

$$p_{TOTALy} = m_A v_{Ay} + m_B v_{By} =$$

Break  $m v_A'$  down into its East-West ( $x$ ) and North-South ( $y$ ) components:

$$m v_{Ax}' =$$

$$m v_{Ay}' =$$

Calculate the East-West ( $x$ ) and North-South ( $y$ ) components of the second ball's momentum:

$$m v_{Bx}' = p_{TOTALx} - m v_{Ax}' =$$

$$m v_{By}' = p_{TOTALy} - m v_{Ay}' =$$

Find the momentum of the second ball (from the components) and the velocity (divide the momentum by the mass):

*Answer:*       $1.7 \text{ m/s } [43^\circ \text{ E of } S]$

2. Two cars collide at an intersection. One car of mass 1400 kg was travelling at 45 km/h [S]. The other car of mass 1300 kg was travelling at 39 km/h [E]. If the cars have a completely inelastic collision, what is their velocity just after the collision?

$$m_A = 1400 \text{ kg} \quad v_A = 45 \frac{\text{km}}{\text{h}} [S] =$$

$$m_B = 1300 \text{ kg} \quad v_B = 39 \frac{\text{km}}{\text{h}} [E] =$$

$$v_{A+B}' = ?$$

Determine the total East-West (x) and North-South (y) components of the momentum before:

$$p_{TOTALx} = m_A v_{Ax} + m_B v_{Bx} =$$

$$p_{TOTALy} = m_A v_{Ay} + m_B v_{By} =$$

Calculate the total momentum of the system before the collision (magnitude and direction):

$$p_{TOTAL} = \quad \theta =$$

Note that  $p_{TOTAL}' = p_{TOTAL}$  .

Calculate the velocity of the cars total after the collision:

$$v_{A+B}' = \frac{p_{TOTAL}'}{m_A + m_B} =$$

*Answer:*  $3.0 \times 10^1 \text{ km/h [39}^\circ \text{ E of S]}$

*Solve the following question on a separate piece of paper:*

3. In a game of marbles, a collision occurs between two marbles of equal mass. One marble is initially at rest; after the collision, the marble acquires a velocity of 1.10 m/s at an angle of  $40.0^\circ$  from the original direction of motion of the other marble, which has a speed of 1.36 m/s after the collision. What is the initial speed of the moving marble?

*Answer:*  $2.00 \text{ m/s}$ . For a full solution, refer to p. 256 – 257.